

## FUNDAMENTALS OF ELECTROMAGNETIC FIELDS – July 11, 2016

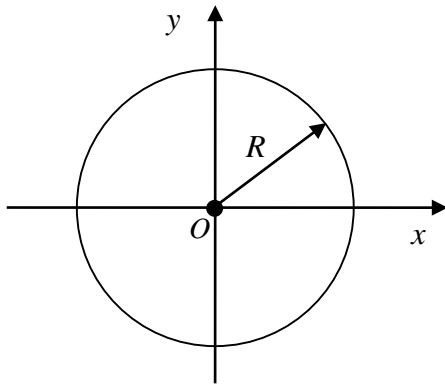
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**Problem 1** - Consider the uniformly charged **cylinder** of radius  $R = 1$  cm in the figure. A charge per unit length  $Q = 0.35$  C/m (charge per unit length) is uniformly distributed over its surface. Calculate

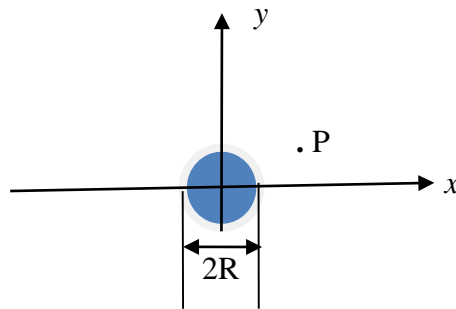
a) the x-component of the electric field at the point P(x=0.3cm, y=0.2cm).

b) the potential at the same point knowing that the potential at  $P_0(x=2\text{cm}, y=0\text{cm})$  is 0.



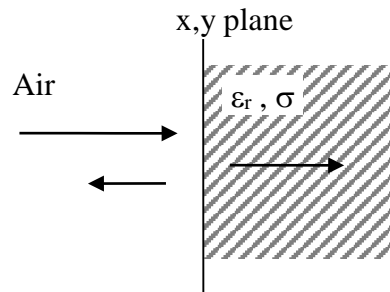
**Problem 2** - Consider the wire in the figure, whose conductivity is  $\sigma = 200 \text{ S/m}$ . It is placed at the origin, its radius  $R$  is 5 mm and it carries a current of 2 A uniformly distributed and directed along  $z$ . Find

- the magnitude and the direction of the magnetic field at  $P(x=1\text{cm}, y=0.5 \text{ cm})$
- the power dissipated on a length of 1 m.



**Problem 3** - A plane wave is incident onto the half-space shown in the figure. The parameters of the half-space are  $\epsilon_r = 3$ ,  $\tan\delta = 0.1$ . The **reflected** power density is  $5 \text{ W/m}^2$  at 2 GHz. Find

- the magnitude of the **incident** electric field (medium 1);
- the magnitude of the **transmitted** magnetic field at 10 cm from the interface.



**Problem 4** - A source with an open circuit voltage  $V_0 = 20 \text{ V}$  and  $R_g = 75 \Omega$  internal impedance is connected to a load  $R_L = 75 \Omega$  by a coaxial line having outer diameter  $a=5 \text{ mm}$ , characteristic impedance  $50 \Omega$  and dielectric constant  $\epsilon_r = 2.2$ ,  $\tan\delta = 0.01$ . The line length is  $l=4 \text{ m}$ , the frequency is  $1 \text{ GHz}$  and the conductors are made with copper ( $\sigma = 5 \cdot 10^7 \text{ S/m}$ ). Find

- The power absorbed by the load;
- The power lost on the line.

